

NUCLEAR



PHYSICS

MASS DEFECT

Mass Defect = $M_{\text{expected}} - M_{\text{observed}}$

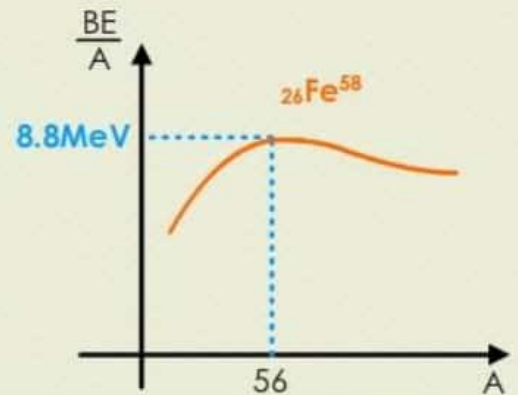
$$\Delta m = [Zm_p + (A - Z)m_n - [M_{\text{atom}} - Zm_e]]$$

BINDING ENERGY

It is the minimum energy required to break the nucleus into its constituent particles.

$$\text{Binding Energy (B.E.)} = \Delta mc^2 = \Delta m \times 931 \text{ MeV}$$

- Binding energy per nucleon is more for medium nuclei than for heavy nuclei. Hence, medium nuclei are highly stable.
- **The heavier nuclei** being unstable have tendency to split into medium nuclei. This process is called **Fission**.
- **The lighter nuclei** being unstable have tendency to fuse into a medium nucleus. This process is called **Fusion**.



RADIOACTIVITY

- It was discovered by **Henry Becquerel**.
- Spontaneous emission of radiations (α , β , γ) from unstable nucleus is called **radioactivity**. Substances which show radioactivity are known as **radioactive substance**.
- **In radioactive decay**, an unstable nucleus emits α particle or β particle. After emission of α or β particle the remaining nucleus may emit γ -particle, and convert into a more stable nucleus.

α - particle

It is a doubly charged helium nucleus. It contains two protons and two neutrons.

$$\text{Mass of } \alpha \text{ - particle} = \text{Mass of } {}_2\text{H} \text{ e}^4 \text{ atom} - 2m_e = 4 m_p$$

$$\text{Charge of } \alpha \text{ - particle} = + 2e$$

β - particle

β^- (electron)

$$\text{Mass} = m_e : \text{Charge} = - e$$

β^+ (positron)

$$\text{Mass} = m_e : \text{Charge} = + e$$

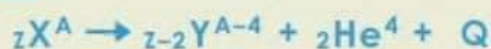
positron is an antiparticle of electron.

γ - particle

They are energetic photons of energy of the order of **MeV** and having zero rest mass.

RADIOACTIVE DECAY (DISPLACEMENT LAW)

1 α - DECAY



Q value is defined as energy released during the decay process.

Q value = rest mass energy of reactants – rest mass energy of products

Let, M_x = mass of atom ${}_Z X^A$, M_y = mass of atom ${}_{Z-2} Y^{A-4}$, M_{He} = mass of atom ${}_2 \text{He}^4$

$$\text{Q value} = [M_x - M_y - M_{\text{He}}] c^2$$

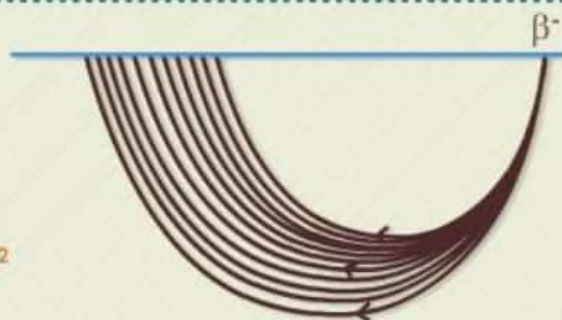


2 β^- - DECAY



$$T_e = \frac{m_y}{m_e + m_y} Q, \quad T_\nu = \frac{m_e}{m_e + m_y} Q,$$

$$\text{Q value} = [M_x - \{(M_y - m_e) + m_e\}] c^2 = [M_x - M_y] c^2$$



3 β^+ - DECAY



$$\text{Q value} = [M_x - \{(M_y + m_e) + m_e\}] c^2 = [M_x - M_y - 2m_e] c^2$$

RADIOACTIVE DECAY : STATISTICAL LAW

- Rate of radioactive decay is directly proportional to N
- where N = number of active nuclei.
- Rate of radioactive decay of $A = \frac{-dN}{dt} = \lambda N$
- where λ = decay constant of the radioactive substance.
- Number of nuclei decayed (i.e., the number of nuclei of B formed)

$$N = N_0 (1 - e^{-\lambda t})$$

1 HALF LIFE ($T_{1/2}$)

$$t_{1/2} = \frac{\ln 2}{\lambda} = \frac{0.693}{\lambda}$$

2 ACTIVITY

Activity is defined as the rate of radioactive decay of nuclei

$$A = A_0 e^{-\lambda t}$$

3 AVERAGE LIFE

$$T_{\text{avg}} = \frac{\text{sum of ages of all the nuclei}}{N_0} = \frac{\int_0^{\infty} \lambda N_0 e^{-\lambda t} dt \cdot t}{N_0} = \frac{1}{\lambda}$$

